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Some Notes on Complexity

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Have a look at the Big-O complexity chart:

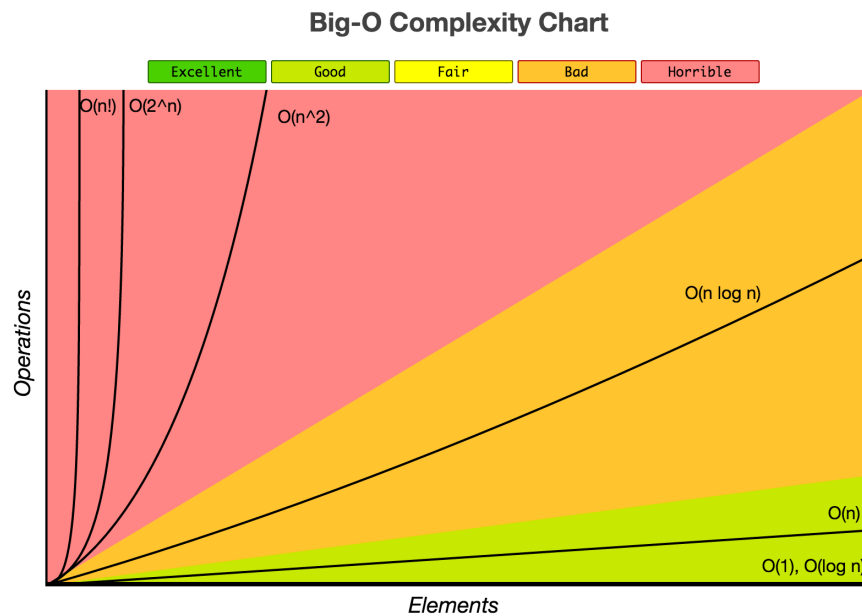


Figure 1: Big-O Complexity Chart

A function has an order, it can be for example

- constant ($O(c)$),
- logarithmic ($O(\log n)$),
- linear ($O(n)$),
- linearithmic ($O(n \log n)$),
- quadratic ($O(n^2)$),
- cubic ($O(n^3)$),
- exponential ($O(c^n)$),
- factorial ($O(n!)$).

This can make a very significant difference, as exemplified in the following code:

```

using System;
using System.IO;

class Program
{
    static int factorial(int n)
    {
        if (n == 0)
            return 1;
        else
            return checked(factorial(n - 1) * n);
    }

    static void Main()
    {
        Console.WriteLine(int.MaxValue);

        int x = int.MaxValue;
        int y = x + 1;
        Console.WriteLine(y);

        try
        {
            y = checked(x + 1);
        }
        catch (System.OverflowException)
        {
            Console.WriteLine("An overflow exception was
↵ thrown.");
        }

        int count0 = 0;
        int n0 = 3;
        try
        {
            while (true)
            {
                count0++;
                n0 = checked(n0 + 1);
            }
        }
        catch (System.OverflowException)
        {
            Console.WriteLine("An overflow exception was
↵ thrown after " + count0 + " iterations.");
        }
    }
}

```

```

        // An overflow exception was thrown after
        ↪ 2147483645 iterations.
    }

    int count1 = 0;
    int n1 = 3;
    try
    {
        while (true)
        {
            count1++;
            n1 = checked(n1 * n1);
        }
    }
    catch (System.OverflowException)
    {
        Console.WriteLine("An overflow exception was
    ↪ thrown after " + count1 + " iterations.");
        // An overflow exception was thrown after 5
        ↪ iterations.
    }

    int count2 = 0;
    int n2 = 3;
    try
    {
        while (true)
        {
            count2++;
            n2 = factorial(n2);
        }
    }
    catch (System.OverflowException)
    {
        Console.WriteLine("An overflow exception was
    ↪ thrown after " + count2 + " iterations.");
        // An overflow exception was thrown after 3
        ↪ iterations.
    }

    int count3 = 0;
    int n3 = 100;
    try
    {
        while (true)
        {

```

```

        count3++;
        n3 = checked(n3 * (int)Math.Log(n3, 2));
    }
    catch (System.OverflowException)
    {
        Console.WriteLine("An overflow exception was
↪ thrown after " + count3 + " iterations.");
        // An overflow exception was thrown after 7
        ↪ iterations.
    }
}

```